

Phase Diagram of the Triangular t - J - K Model in the Doped-Mott Region:

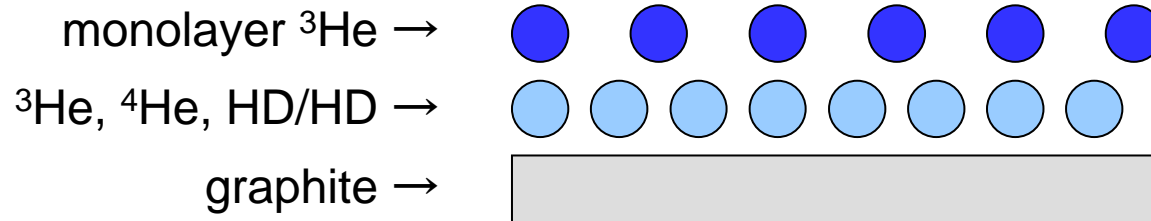
Effects of Ring Exchange Interactions and the
“Spin-Charge Separation”

Masao Ogata (Univ. of Tokyo)

Yuki Fuseya (Osaka Univ.)

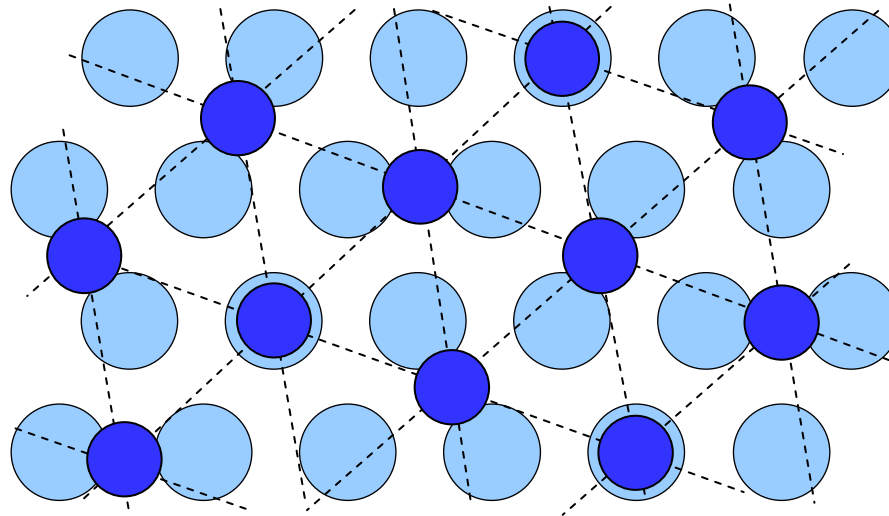
J. Phys. Soc. Japan 78, 013601 (2009)

^3He adsorbed on graphite



Triangular lattice

“half-filling”



localization at

“4/7 phase”

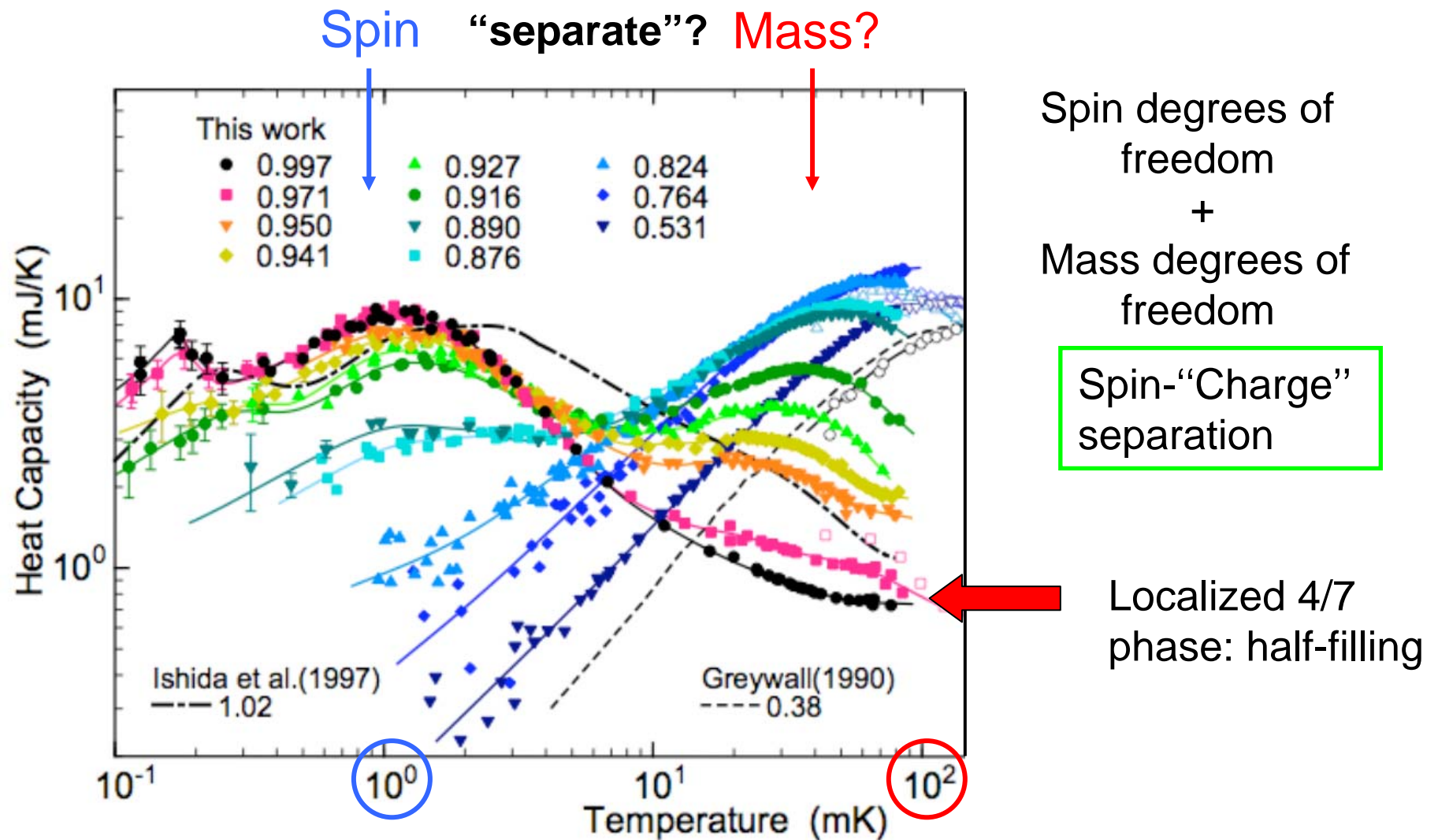
2D ^3He : underlayer

- Strongly correlated Fermion system
- Purely two-dimensional
- Super Clean

[Elser (1989)]

= 4 : 7

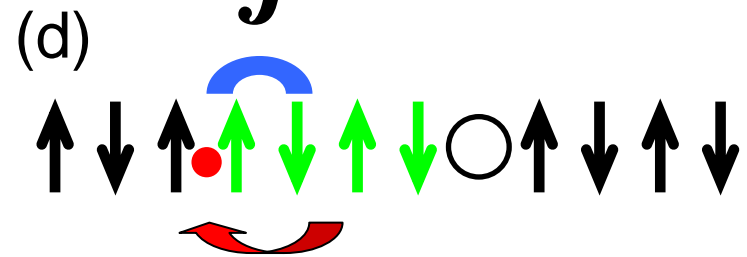
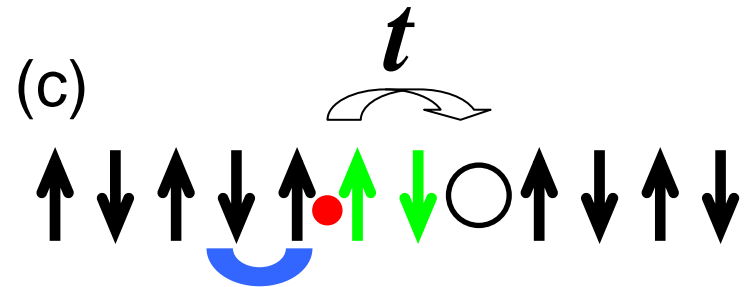
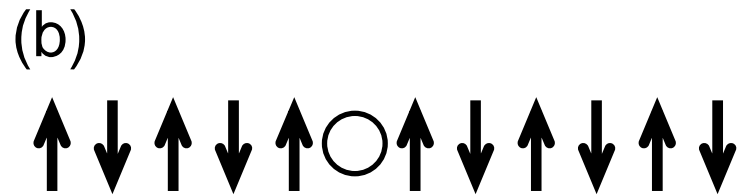
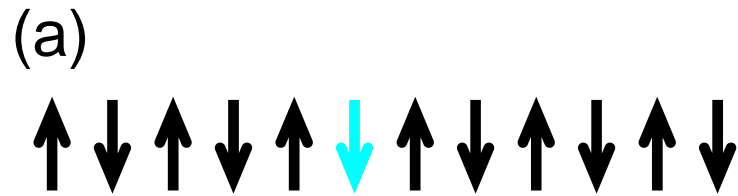
Double-peaked heat capacity



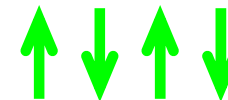
³He/⁴He/gr, [Matsumoto, et al. (2007)]

Spin-Charge separation in 1-dim

Tomonaga-Luttinger liquid



In 2-dim ---- movement of a hole leaves
 trace of **Unfolded** spin states
 spin - charge binding
 Fermi Liquid



t - J model as a model for ^3He

A model of monolayer ^3He in the doped case

Large U Hubbard model = t - J model

in a triangular lattice ----- Frustration

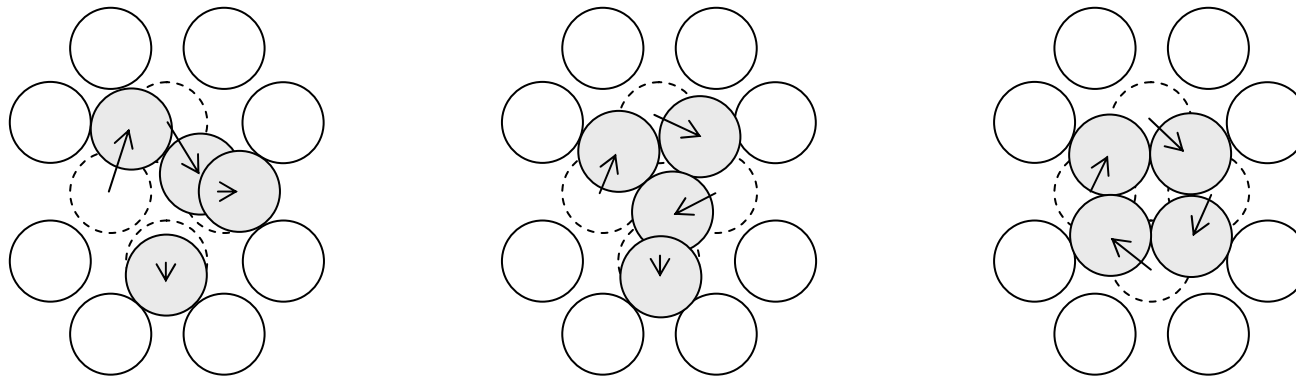
$$H = -t \sum_{i,j,\sigma} \left(\tilde{c}_{i\sigma}^\dagger \tilde{c}_{j\sigma} + \text{H.c.} \right) \\ + J \sum_{i,j} \left(\mathbf{S}_i \cdot \mathbf{S}_j - \frac{1}{4} n_i n_j \right)$$

However, no spin-charge separation was observed in the triangular t - J model. (Koretsune-Ogata, PRL 89, 116401 (2002))

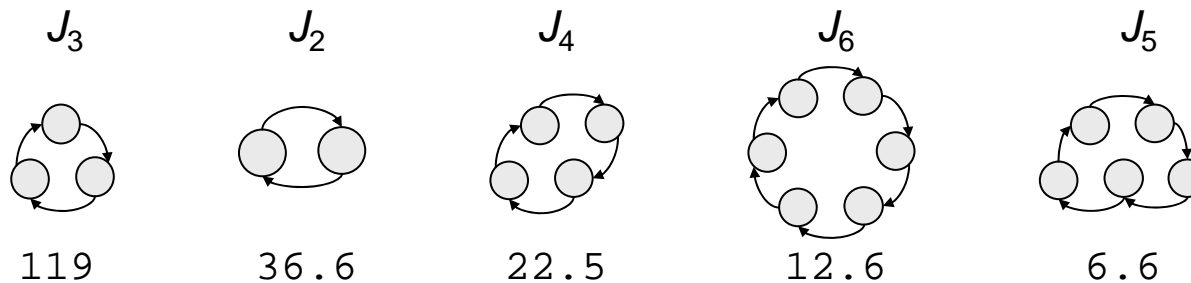
Multiple Spin Exchange

MSE is relevant in a hard-core quantum solid

--- Thouless (1965)



$$H = \sum_n (-1)^n J_n (P_n + P_n^{-1})$$



[Bernu et al. (1992)]

t - J - K model

As a minimum model of monolayer ^3He , we use

t - J - K model

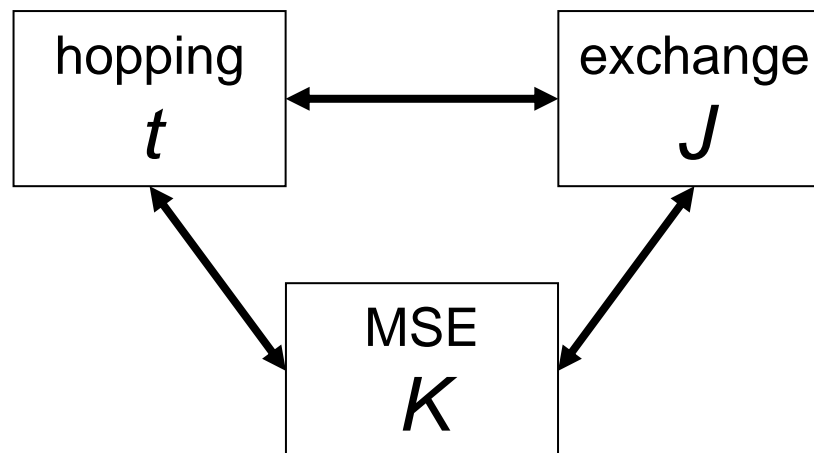
$$H = -t \sum_{i,j,\sigma} \left(\tilde{c}_{i\sigma}^\dagger \tilde{c}_{j\sigma} + \text{H.c.} \right)$$

$$J = J_2 - 2J_3$$

(J can be ferro. for large J_3)

$$+ J \sum_{i,j} \left(\mathbf{S}_i \cdot \mathbf{S}_j - \frac{1}{4} n_i n_j \right) + K \sum_{i,j,k,l} (P_4 + P_4^{-1})$$

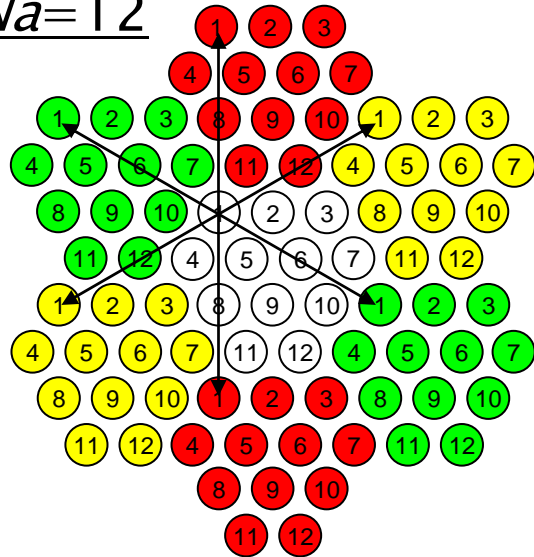
$$(J = J_2 - 2J_3)$$



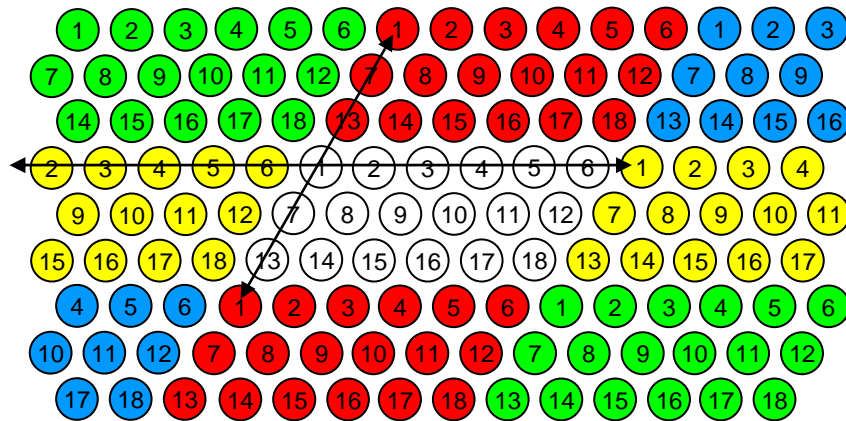
Cluster

Exact diagonalization

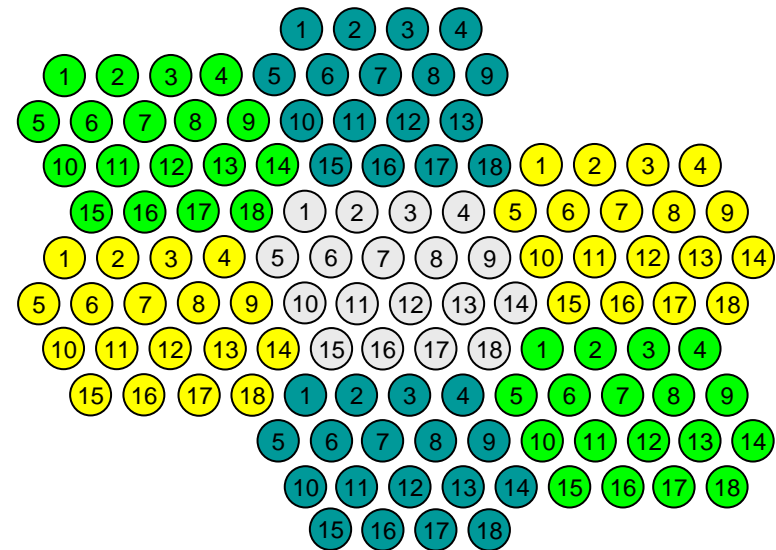
$Na=12$



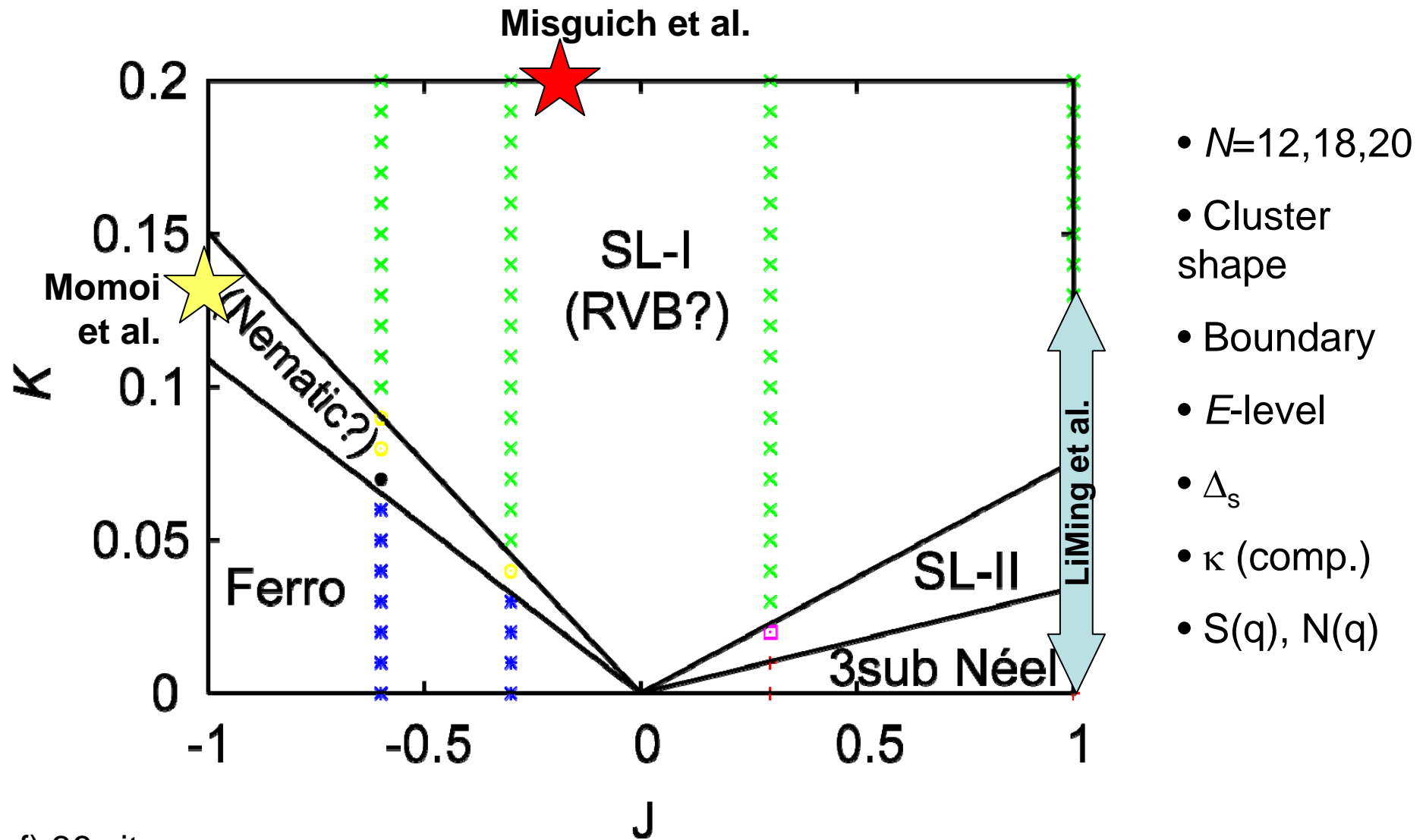
$Na=18a$



$Na=18b$



Half filling ($n=1.0$)



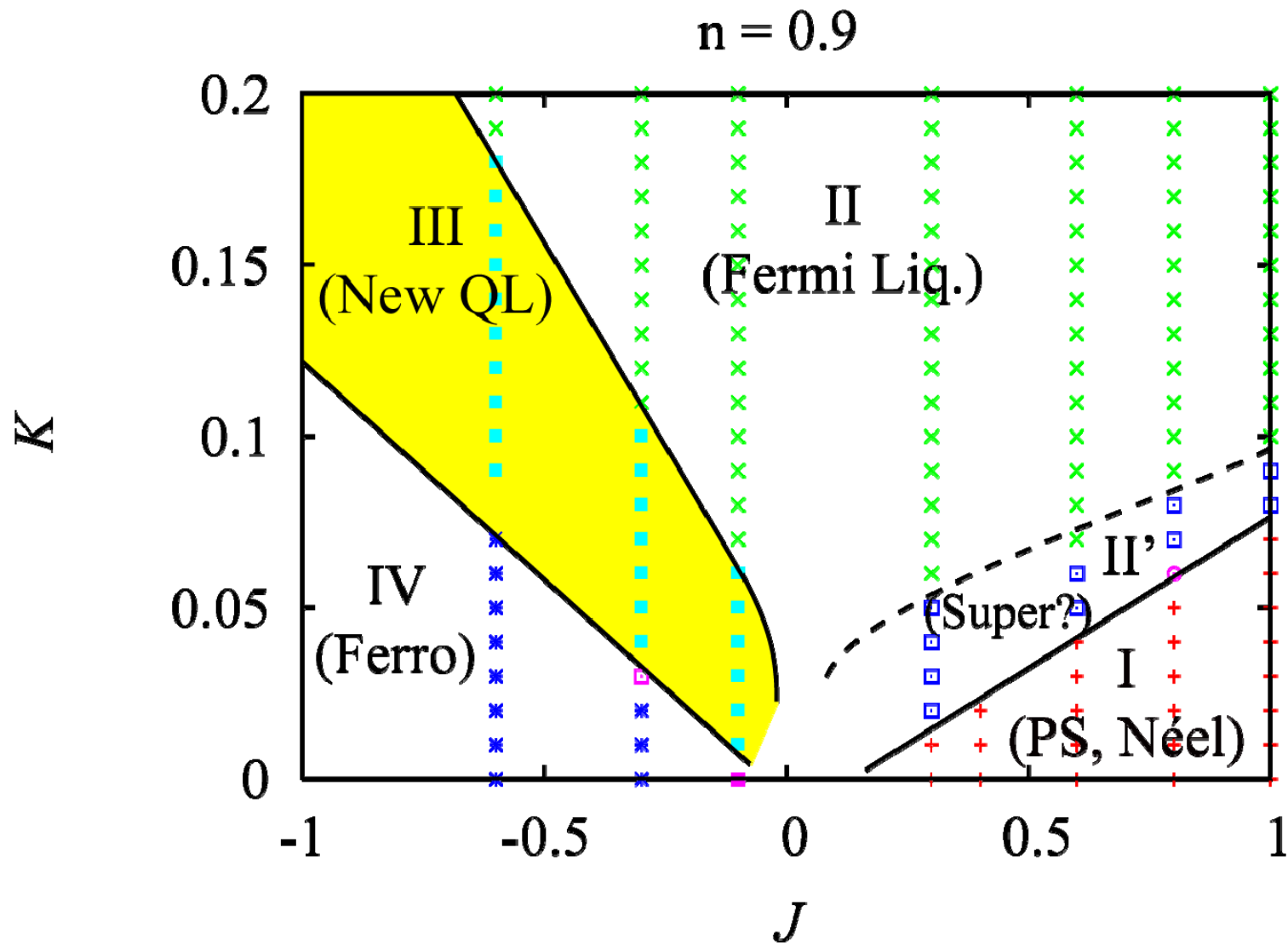
- $N=12,18,20$
- Cluster shape
- Boundary
- E -level
- Δ_s
- κ (comp.)
- $S(q), N(q)$

cf) 36 site

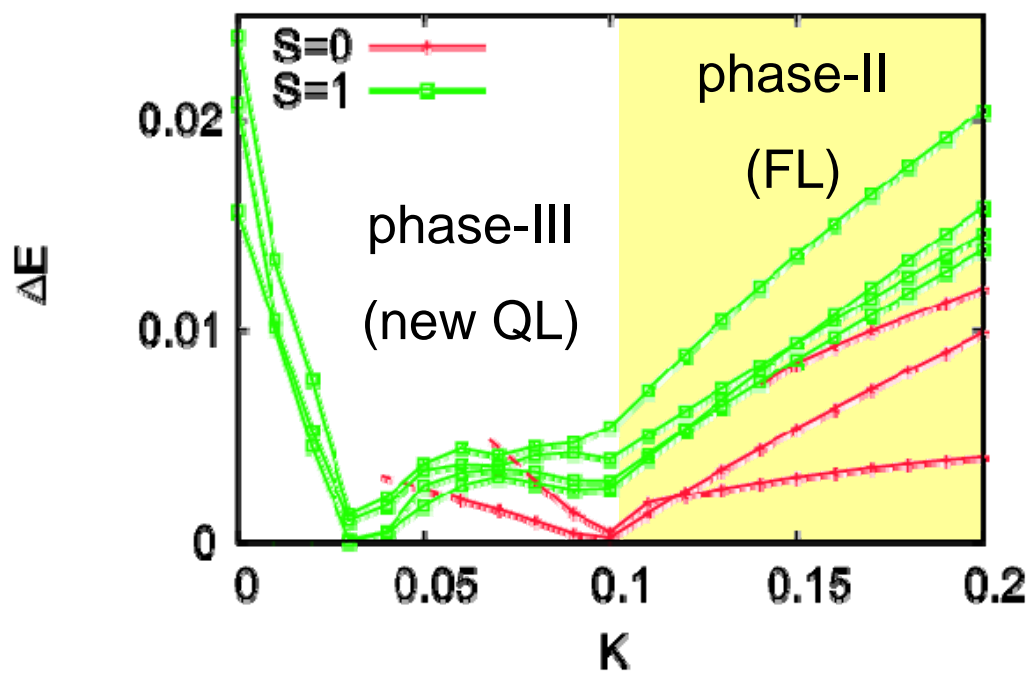
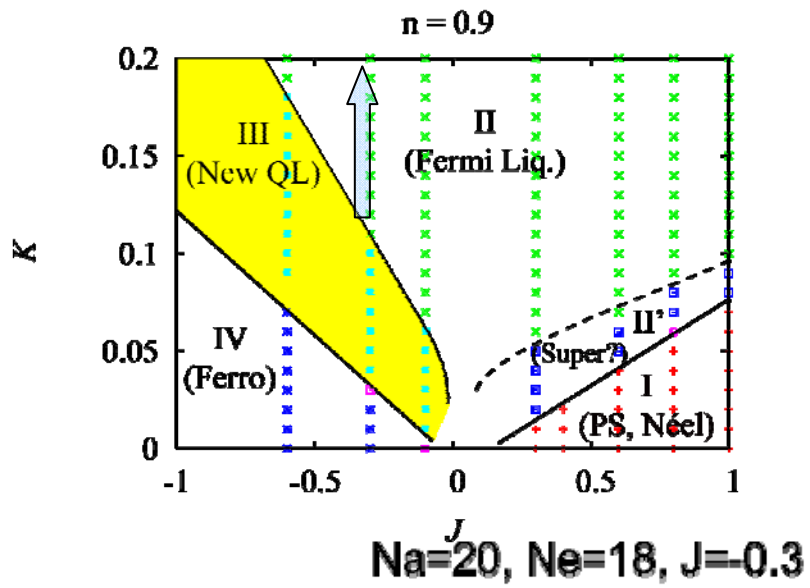
Misguich, et al (1999)

LiMing, et al (2000) Momoi et al (2006)

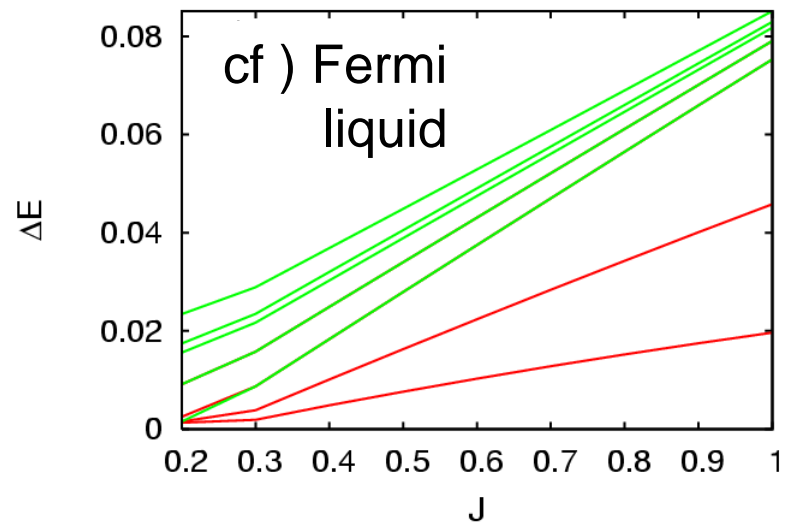
Doped region ($n=0.9$)



Excitation energy



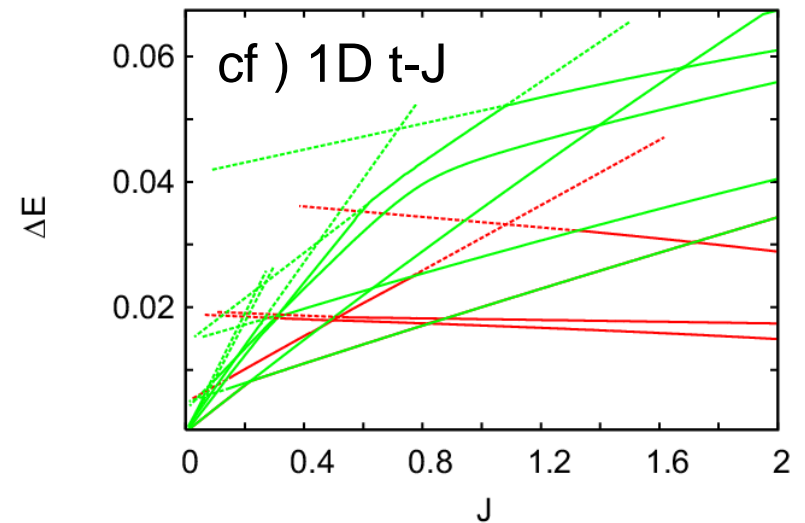
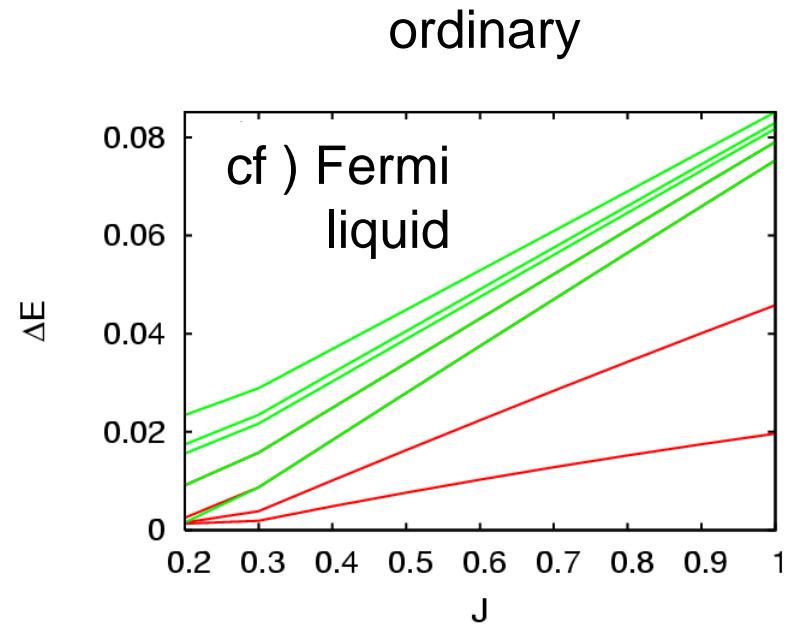
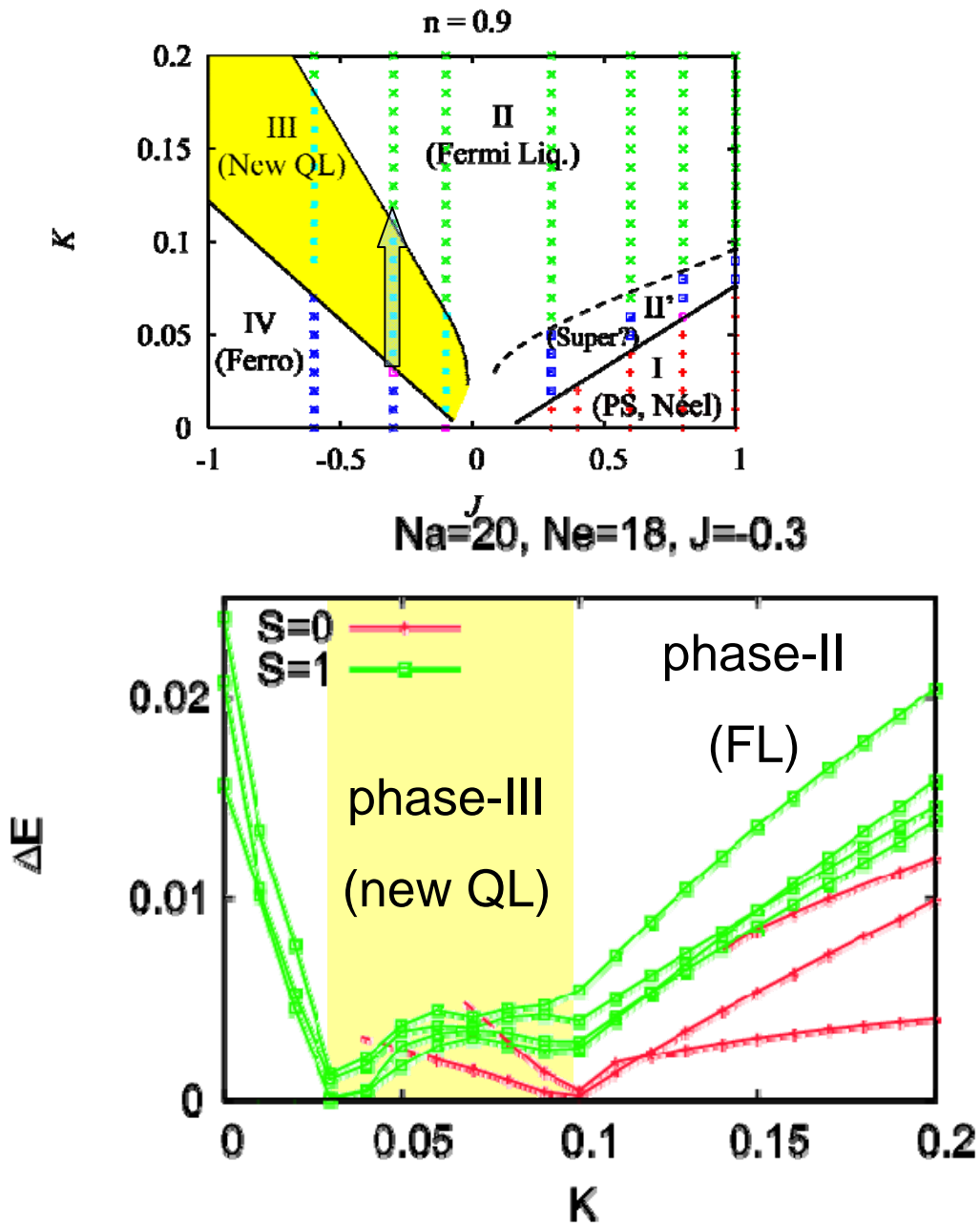
ordinary



Fermi Liquid region

$S(q)$ and $N(q)$ are consistent with Fermi surface

Excitation energy



Spin-Charge separation in 1-dim

Tomonaga-Luttinger liquid

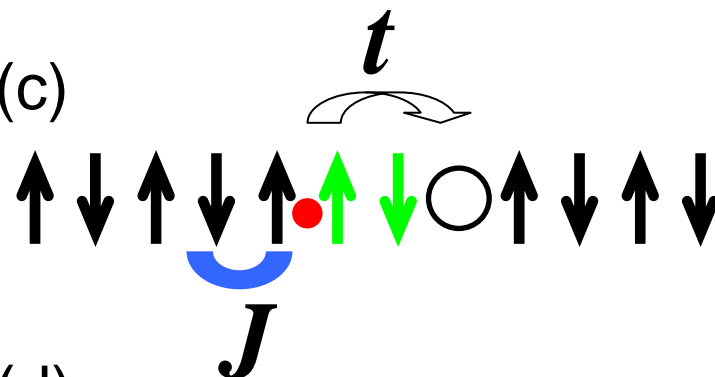
(a)



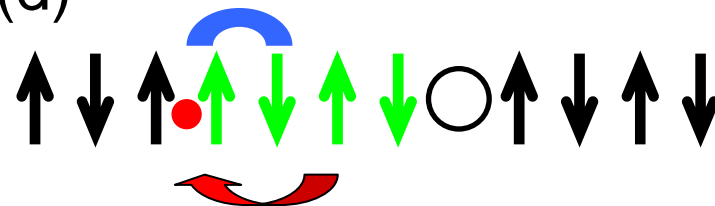
(b)



(c)

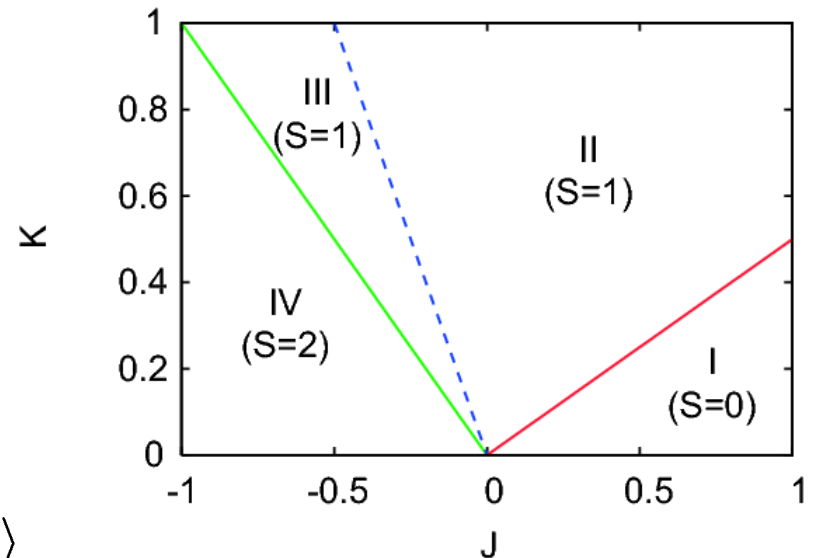
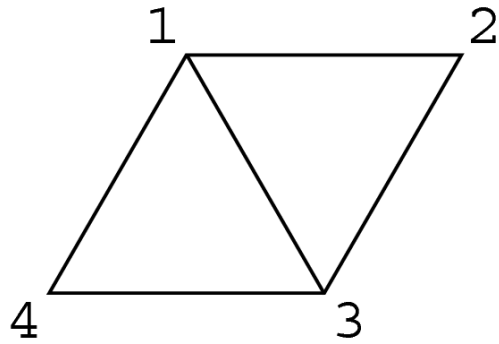


(d)



Similar situation can be considered in the t - J - K model !

4-site cluster



S=0

$$-J + 2K \quad |\uparrow\uparrow\downarrow\downarrow + \downarrow\downarrow\uparrow\uparrow + \uparrow\downarrow\downarrow\uparrow + \downarrow\uparrow\uparrow\downarrow - 2\uparrow\downarrow\uparrow\downarrow - 2\downarrow\uparrow\downarrow\uparrow\rangle$$

S=1

$$J \quad |\uparrow\uparrow\downarrow\uparrow - \downarrow\uparrow\uparrow\uparrow\rangle$$

$$3J \quad |\uparrow\uparrow\uparrow\downarrow - \uparrow\downarrow\uparrow\uparrow\rangle$$

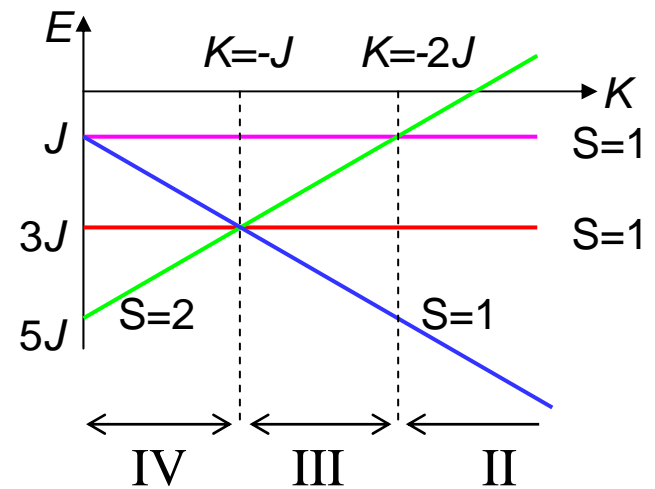
$$J - 2K \quad |\uparrow\uparrow\uparrow\downarrow - \uparrow\uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\uparrow - \downarrow\uparrow\uparrow\uparrow\rangle$$

S=2

$$5J + 2K \quad |\uparrow\uparrow\uparrow\uparrow\rangle$$

K (ring) dominant case

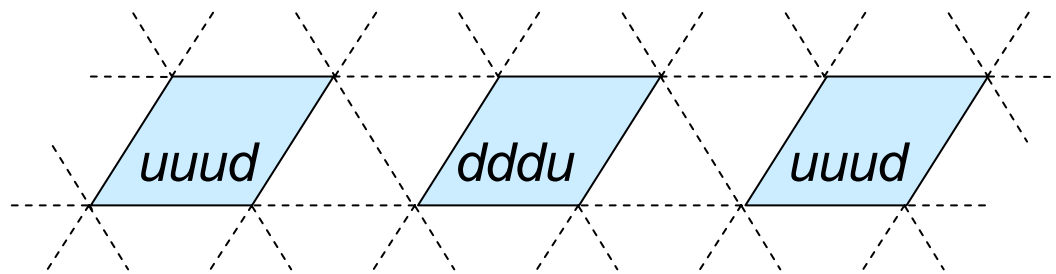
J (<0) dominant case (Ferro)



Plaquette approximation

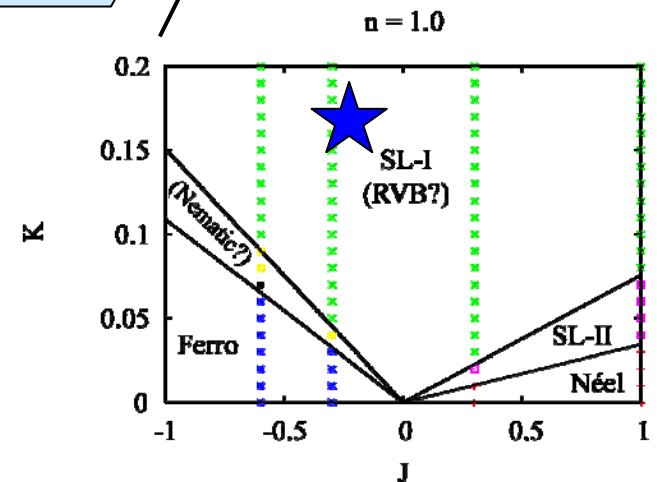
K-dominant case $|\uparrow\uparrow\uparrow\downarrow - \uparrow\uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\uparrow - \downarrow\uparrow\uparrow\uparrow\rangle \quad J - 2K$

SL-I RVB: $\left| \begin{array}{cc} \text{uuud} & \text{dddu} \\ \text{dddu} & \text{uuud} \end{array} \right\rangle$

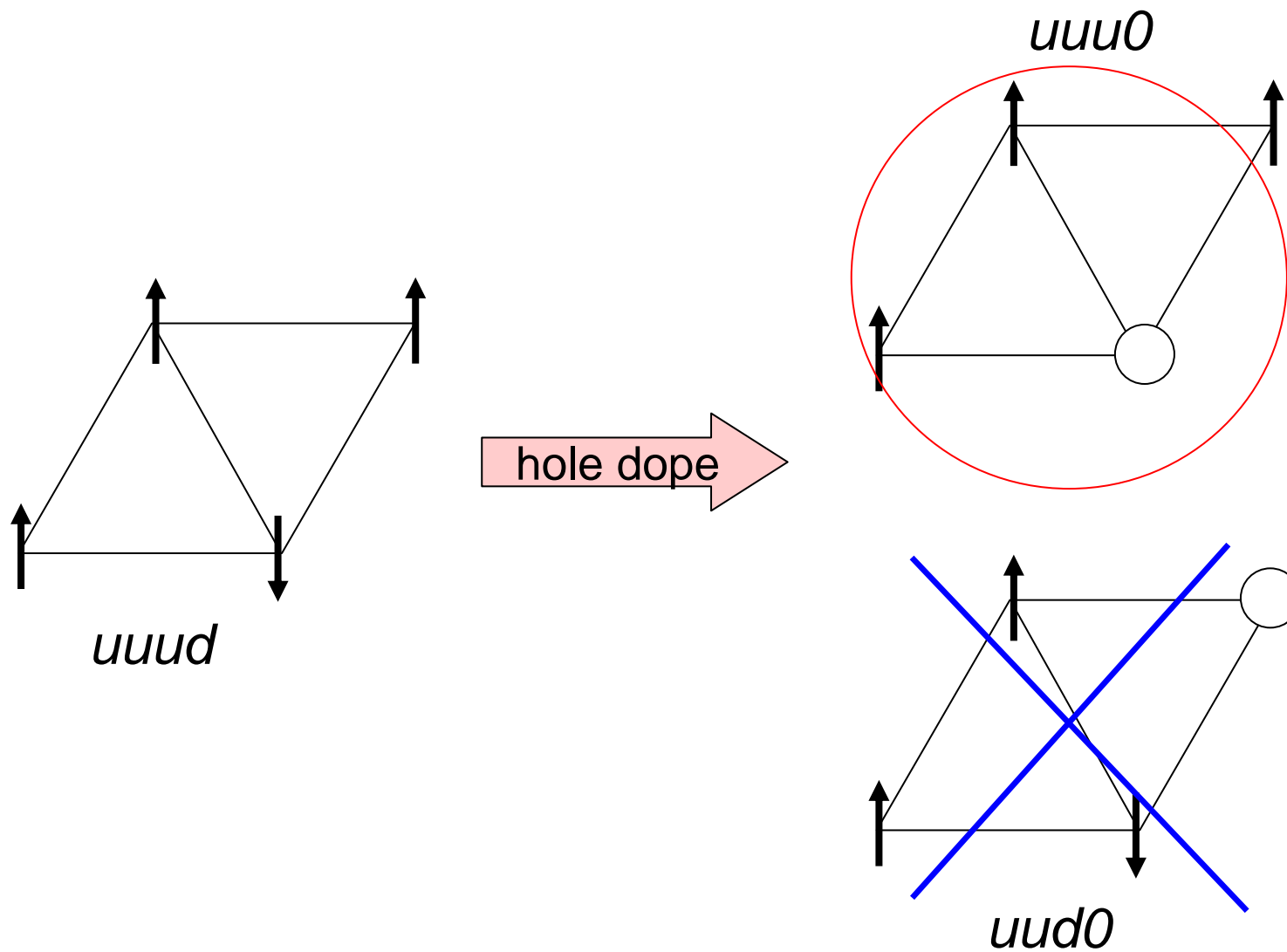


$$|\uparrow\uparrow\uparrow\downarrow - \uparrow\uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\uparrow - \downarrow\uparrow\uparrow\uparrow\rangle = \text{uuud}$$

u3d1 state



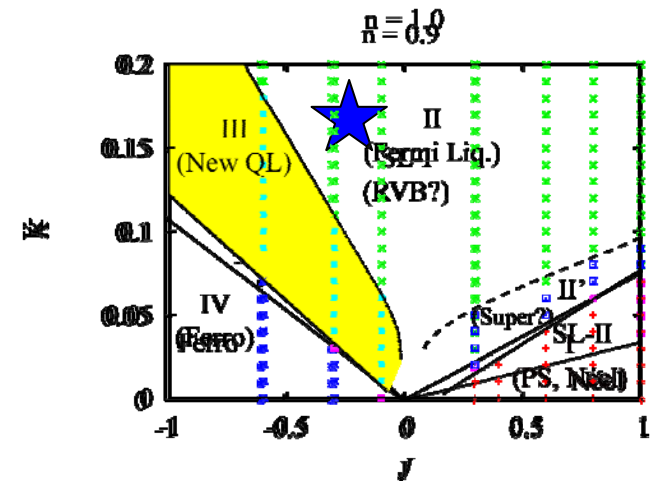
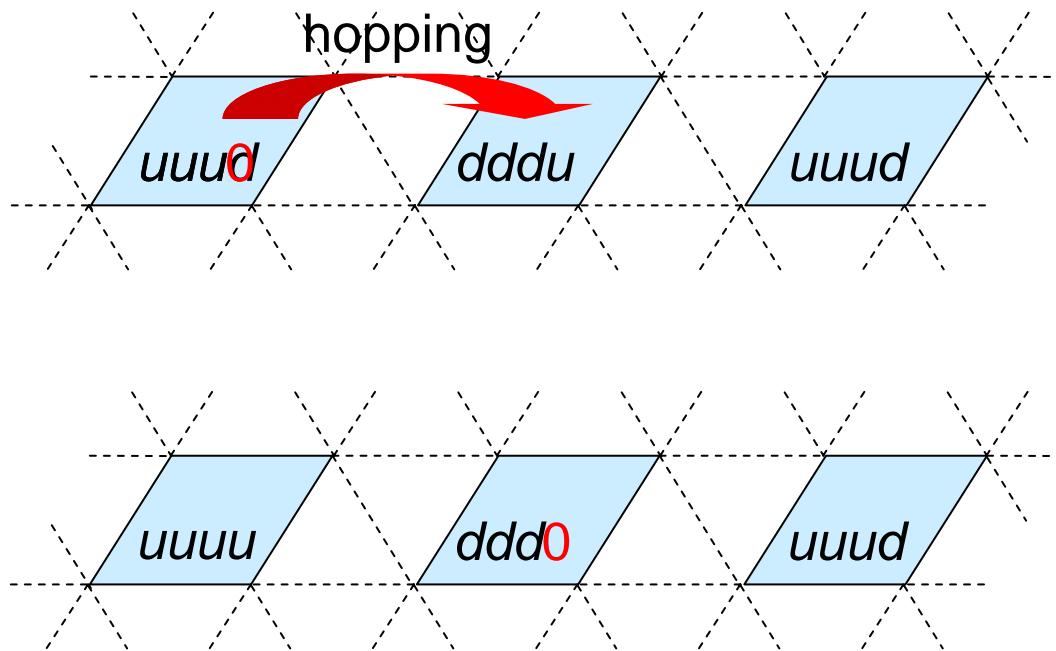
Hole-doped plaquette



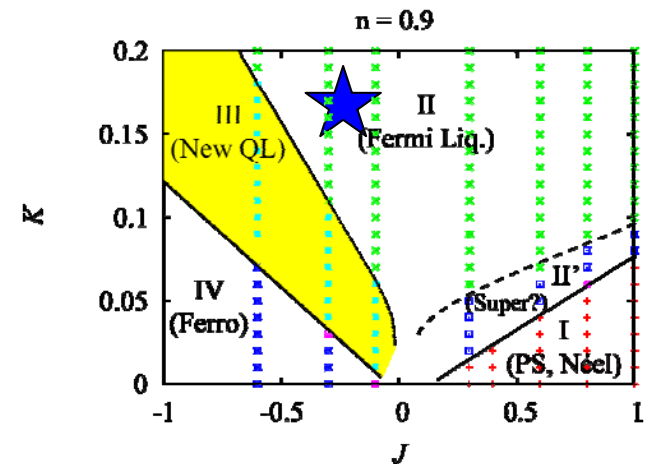
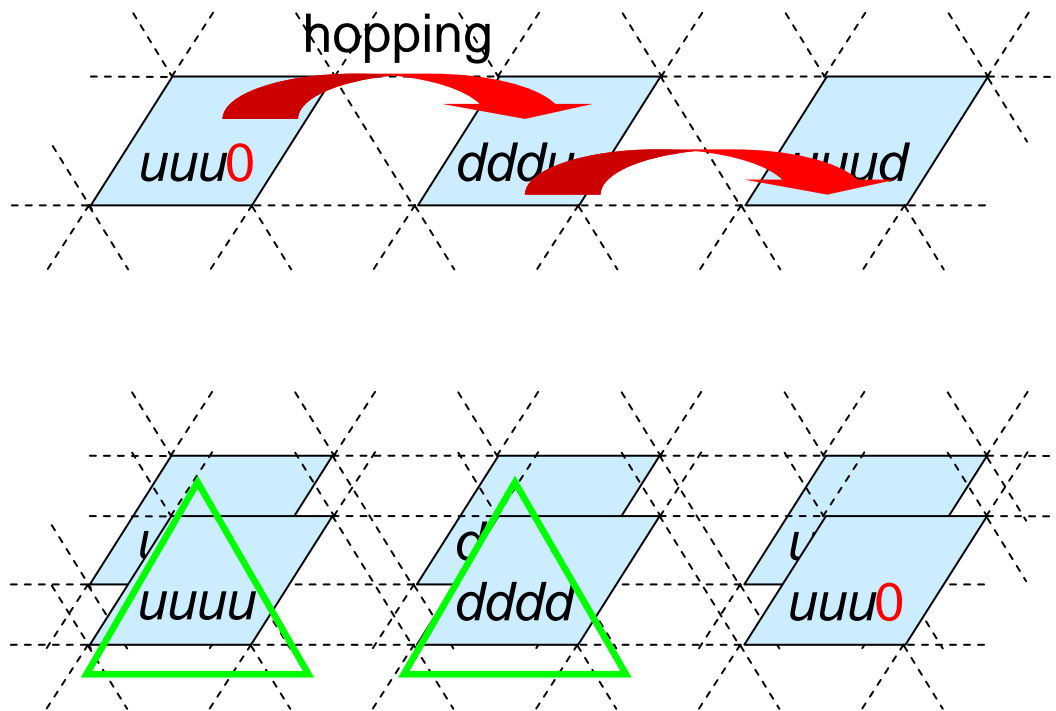
Plaquette approximation

K-dominant case $|\uparrow\uparrow\uparrow\downarrow - \uparrow\uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\uparrow - \downarrow\uparrow\uparrow\uparrow\rangle \quad J - 2K$

Hole doping



Plaquette approximation



hole motion

Unfavored spin states remains. \Rightarrow spin-charge binding: Fermi liquid

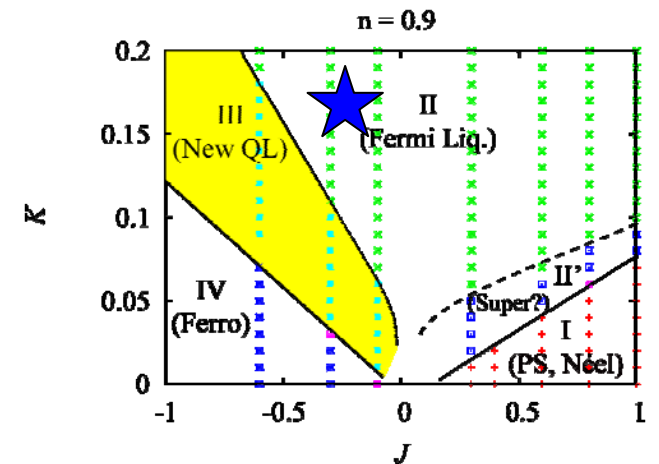
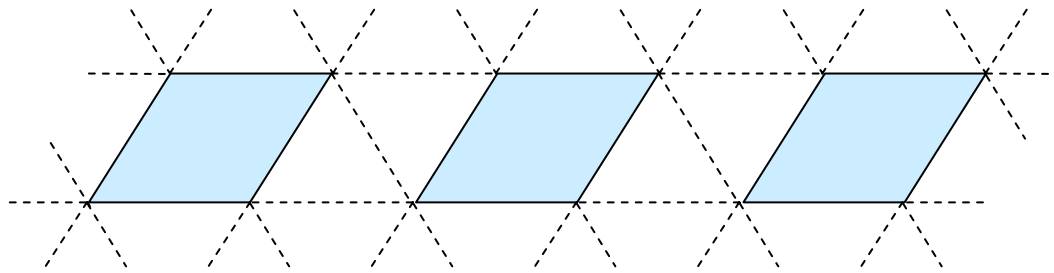
Plaquette approximation

***J-K*-competing case**

$$|\uparrow\uparrow\uparrow\downarrow - \uparrow\uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\uparrow - \downarrow\uparrow\uparrow\uparrow\rangle \quad uuud$$

$$\text{almost degenerate } |\uparrow\uparrow\uparrow\uparrow\rangle \quad \underline{uuuu}$$

Hole doping



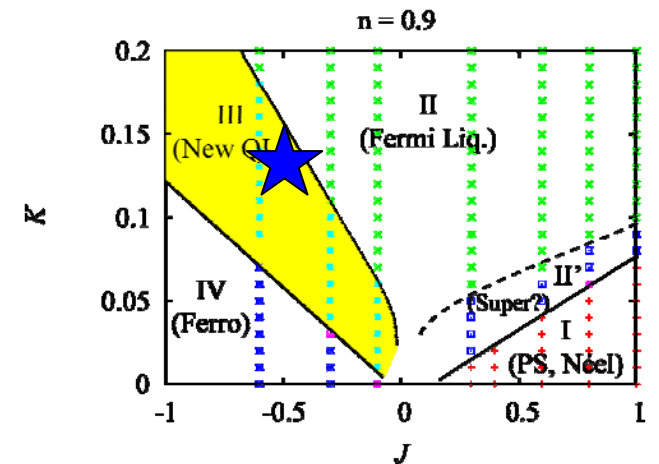
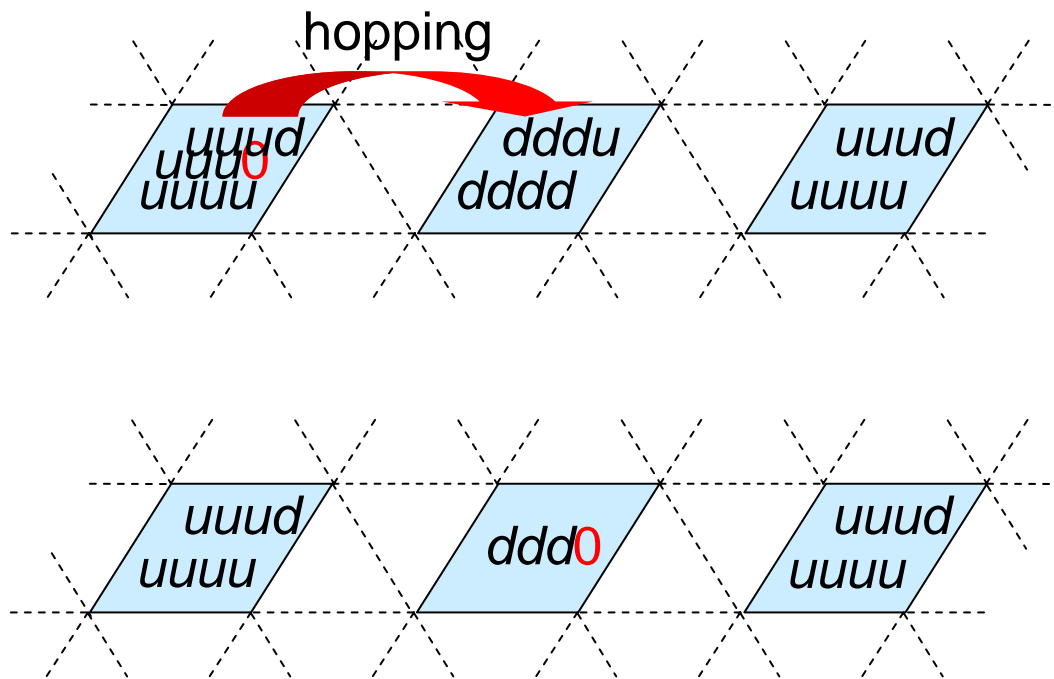
Plaquette approximation

J-K-competing case

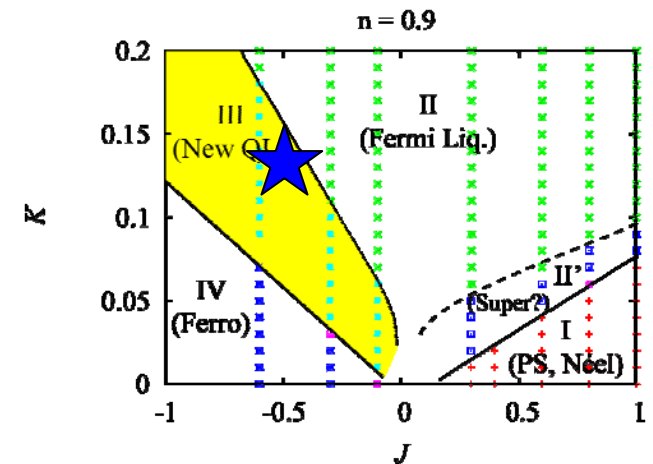
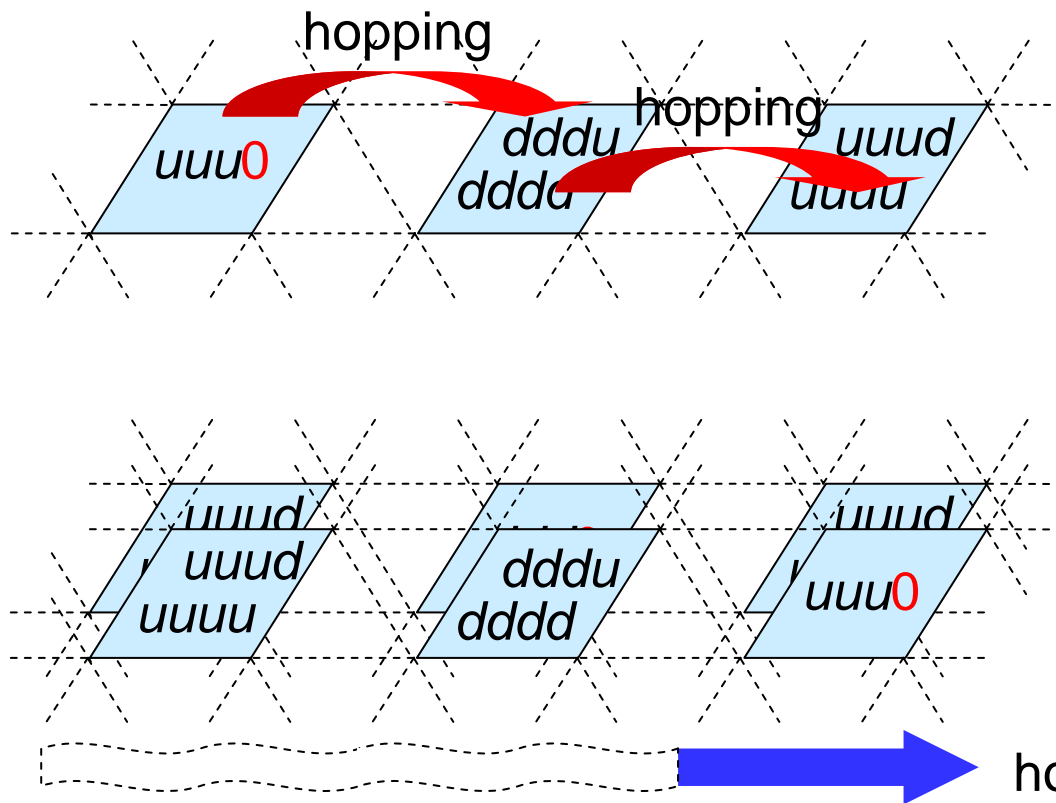
$$|\uparrow\uparrow\uparrow\downarrow - \uparrow\uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\uparrow - \downarrow\uparrow\uparrow\uparrow\rangle \quad uuud$$

$$|\uparrow\uparrow\uparrow\uparrow\rangle \quad uuuu$$

Hole doping



Plaquette approximation

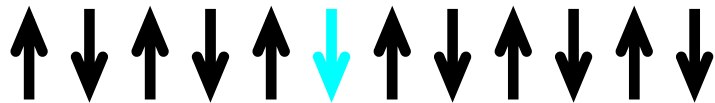


No trace of spin \Rightarrow spin-charge separation as in 1-dim : new state

Spin-Charge separation in 1-dim

Tomonaga-Luttinger liquid

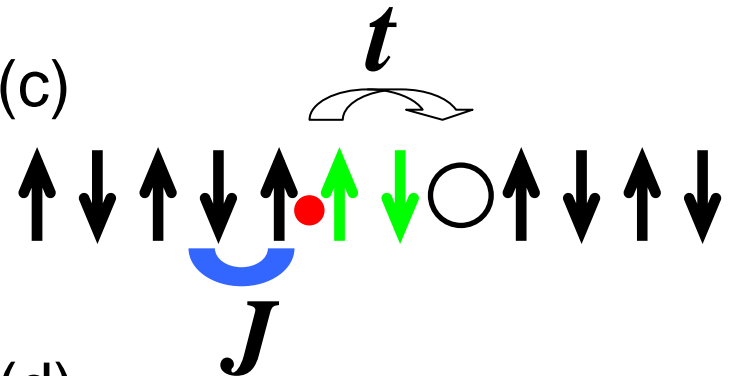
(a)



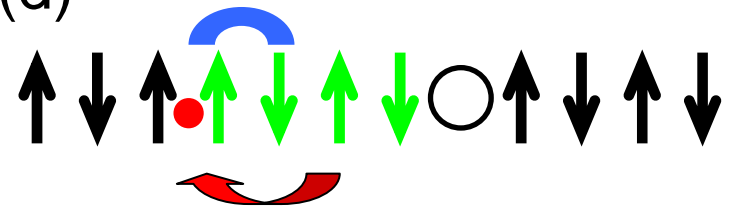
(b)



(c)

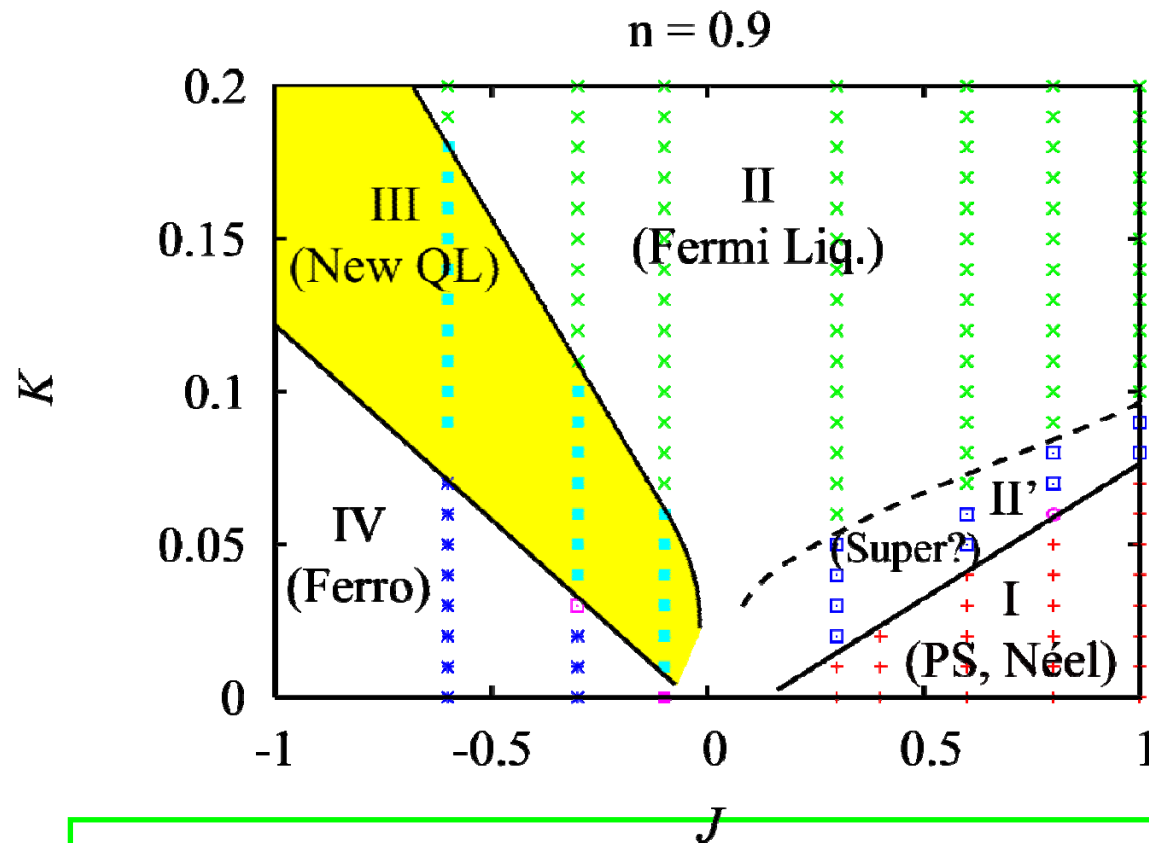


(d)



Similar situation in the t - J - K model

Summary



Fuseya-Ogata:
arXiv: 0804.4329
(JPSJ 78, 013601 (2009))

Doping dependence
will be OK.

- **Triangular t - J - K model** (exact diagonalization, up to 20 site)
- **New state** (between Ferro and Fermi liquid)
- **Spin-charge separation** (J vs. K , consistent with 2D ^3He double peak in C)